

1. Please answer the following questions about the circuit in Fig. 1.

- (a) (10%) Suppose  $E_1 = E_2 = 10 \cos(10t)$ ,  $R_1 = R_2 = \infty$ ,  $L = 2$  H and  $C = 0.02$  F, and initially  $i(0) = 1$  A and  $v(0) = 0$ , what is the amplitude and oscillation frequency of the voltage  $v(t)$  across the capacitor?
- (b) (10%) Suppose  $E_1 = E_2 = 10 \cos(10t)$ ,  $R_1 = R_2 = 1\Omega$ ,  $L = 2$  H and  $C = 0.02$  F, and initially  $i(0) = 1$  A and  $v(0) = 0$ , what is the current  $i(t)$  through the inductor in steady state?
- (c) (10%) Suppose  $E_1 = 10 \cos(10t)$ ,  $E_2 = 10 \sin(20t)$ ,  $R_1 = R_2 = 1\Omega$ ,  $L = 2$  H and  $C = 0.02$  F, and initially  $i(0) = 1$  A and  $v(0) = 0$ , what is the average power dissipation on resistor  $R_2$ ?
- (d) (10%) Suppose  $E_1 = 10 \cos(10t)$ ,  $E_2 = 0$ ,  $R_1 = 1\Omega$ , and  $C = 0.02$  F, what the values of  $L$  and  $R_2$  should be chosen to achieve maximum average power delivered to resistor  $R_2$ ? Also, what is the maximum average power delivered to  $R_2$ ?
- (e) (10%) Suppose  $R_1 = R_2 = 1\Omega$ ,  $L = 2$  H and  $C = 0.02$  F, what is the transfer function  $E_1$  to  $i$ ?

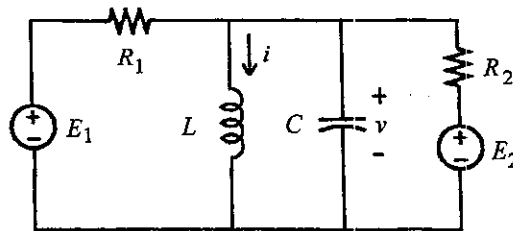


Fig. 1

2. (10%) For the transformer with  $L_1 = 0.001$  H,  $L_2 = 0.1$  H,  $M = 0.01$  H, and  $R = 10$  ohm, shown in Fig. 2, please find its input impedance function  $Z(s)$ .

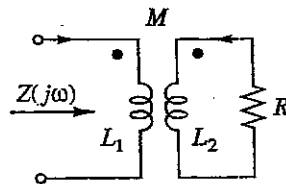


Fig. 2

3. For the circuit in Fig. 3, please answer the following question,
- (10%) If the voltage across the capacitor is initially 1 volt, then, given input voltage  $v_s = 2\sin(0.5t)$ , what is the output voltage  $v_o(t)$ ?
  - (10%) Is the active filter shown below highpass or lowpass? What is its cutoff frequency?
  - (10%) Scale the resistors and capacitor such that the resulting input impedance is 1000 times larger than the original one while maintaining the same transfer function.

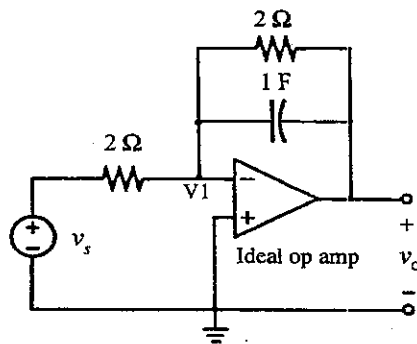


Fig. 3

4. (10%) Assume the equivalent circuit for the coil shown in Fig. 4 is a  $2\Omega$  resistor and  $10\text{mH}$  inductor in series. Suppose the switch is closed for a long time, then what is the amount of energy stored in the coil? If the switch opened suddenly, would the voltage on the terminal B rise or fall?

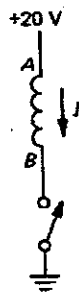


Fig. 4