

國立中山大學 103 學年度碩士暨碩士專班招生考試試題

科目名稱：工程數學【光電所碩士班】

題號：435001

※本科目依簡章規定「可以」使用計算機（廠牌、功能不拘）

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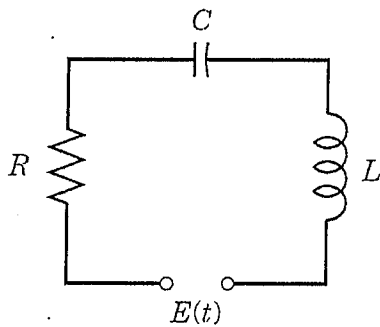
1. Solve the IVP. Show the steps of derivation, beginning with the general solution. (10 points)
 $y' = -4x/y, y(2) = 3$

2. Find a real general solution. Show the details of your work. (10 points)
 $xy'' + 4y' = 0$

3. Is the given function below linearly dependent or independent on the half-axis $x \geq 0$? Give reason. (15 points)

$$e^{-x} \cos x, e^{-x} \sin x, e^{-x}$$

4. Using the Laplace transform to solve RLC-circuit problems. Find the current $E(t)$ in the circuit, assuming zero initial current and charge. (25 points)



$$R = 2\Omega, L = 1H, C = 0.5 F, E(t) = 1 \text{ kV if } 0 < t < 2 \text{ and } 0 \text{ if } t > 2.$$

5. Find (a) the Fourier cosine series (8 points), (b) the Fourier sine series. (7 points)
 $f(x) = \sin x \quad (0 < x < \pi)$

6. By the principles used in modeling the string it can be shown that small free vertical vibrations of a uniform elastic beam are modeled by the fourth-order PDE.

$$\frac{\partial^2 u}{\partial t^2} = -c^2 \frac{\partial^4 u}{\partial x^4}$$

(a) find solutions $u_n = F_n(x)G_n(t)$ corresponding to zero initial velocity and satisfying the boundary conditions: $u(0,t) = 0, u(L,t) = 0, u_{xx}(0,t) = 0, u_{xx}(L,t) = 0$ (12 points)

(b) find the solution that satisfies the conditions in (a) as well as the initial condition: $u(x,0) = f(x) = x(L-x)$. (13 points)

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科目名稱：電磁學【光電所碩士班】

題號：435002

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一、 填充題：每格 5 分，a-o 共十五格，占 75 分

1. 考慮一個非均勻半徑為 r 之帶電球體，其電荷分佈在半徑 R 小於等於 r 時為 $\rho_0 \left(1 - \frac{R^2}{r^2}\right)$ ，其餘地區為 0。請問球內總電荷為 a、球內電場分佈為 b。
2. 接上題，若改為均勻帶電球體，此時之電荷分佈為 ρ_0 ，請問球外靜電場分佈為 c、電位分佈為 d。
3. 點電荷 $+Q$ ，放於大內外半徑分別是 a 、 b 且介電係數為 ϵ 的球型介電球殼，請問離球心距 r 為 a 到 b 的介電材料範圍中的電場 E 為 e、極化相量 P 為 f。另外，請問體積電荷密度 ρ_{pv} 為 g。
4. 考慮兩個大小相同半徑為 r 金屬球距離 d 遠大於 r ，其球間電容為 h。
5. 面積為 A ，相距為 d 的平行板電容其電壓充電到 V 能儲存的電位能 i。
6. 半徑 a 之接地金屬球與距其球心距 b (註： $b > a$) 之電荷 Q 之間吸引力為 j。
7. 在自由空間中，一個半徑 a 之金屬球放在方向為 z 軸之電場 E 所感應出之 dipole moment 為 k、電位為 l。
8. 半徑為 a 、面電荷密度是均勻且值為 ρ_s 之圓盤，若以 ω 角速度旋轉，請問圓盤中心的磁通密度 B_0 為 m。
9. 一條載有直流電流 I 得長直導線 (半徑 r 、導電率 σ)，請問導線表面 Poynting vector 方向為 n，大小為 o。

二、 簡答與計算題；共兩題，共二十五分。

1. 試證明電磁波是橫波 (5 分)
2. 何謂肌膚深度 (skin depth)? (5 分)，為何有白銀與黃金的說法? (5 分)，海水中用 1MHz 的電磁波其穿透深度為 0.25 公尺，若考慮深海 (折射率 1.5) 探測攝影想利用綠光 (於攝影機上且波長為 500nm) 觀測，若其容忍的衰減是 30dB 請問攝影機距探測目標最多多遠? (10 分)

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科目名稱：近代物理【光電所碩士班選考】

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I. Questions: (60%)

1. Please show that the phase velocity and the group velocity of an electromagnetic wave propagating in free space are equal. (5%)
2. An electron and a proton are accelerated from rest through a total potential energy difference of 1.6×10^{-11} J. What is the increase in mass and final speed of each particle? (7%)
3. What is the threshold wavelength for a cathode material of 3.75 V stopping potential, if the incident light has a momentum of 3.32×10^{-27} kg·m/s? (7%)
4. What are the phase velocity and wavelength of a proton moving at a particle speed of (a) 10^2 m/s, and (b) 2×10^8 m/s? (7%)
5. An X-ray photon of 0.05 nm wavelength strikes a free, stationary electron. The photon scatters at 90° . Determine the momentum of the incident photon and the scattered photon. The Compton wavelength λ_C is 0.00243 nm. (5%)
6. An electron traveling at 8×10^6 m/s enters the region of the Thomson e/m_e apparatus where E and B fields coexist and are adjusted to be counter balancing. The E field is created by a parallel plate connected to a 91.1 V battery and having a 6.4 cm plate separation. If the E field is deactivated, what is the radius of the electron's circular arc through the counter balancing magnetic field? (7%)
7. Using the generalized equations for the Bohr radii and Bohr velocities, please find the principal quantum number and translational speed of an electron encircling a single fixed proton with a 1 m radius. The Bohr radius is 0.53 Å. (5%)
8. A typical atomic nucleus is about 10^{-14} m in radius. What is the lower limit of the momentum of an electron must have if it is to be part of a nucleus? (5%)
9. Please tell the differences between fluorescence and phosphorescence of excited molecules. (5%)
10. Using the de Broglie's and Schrödinger's postulates together with the free particle wave function $\Psi(x,t) = Ae^{j(kx-\omega t)}$, please construct the Schrödinger's one dimensional time-dependent wave equation. (7%)

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II. Problems: (40%)

1. Assuming a cubic meter of hydrogen at 0°C and at atmospheric pressure satisfies Maxwell-Boltzmann statistics ($f_{MB}(\varepsilon) = Ae^{-\varepsilon/kT}$, where A is a constant, and T is ambient temperature). This system contains about 2.7×10^{25} atoms and the number of the atoms of energy ε within the system can be expressed by

$$n(\varepsilon) = g(\varepsilon) \times f_{MB}(\varepsilon),$$

where $g(\varepsilon)$ is number of states at energy ε and $f_{MB}(\varepsilon)$ is the probability of occupancy of the state at energy ε . Please find the number of these atoms in their first excited states ($n = 2$) at 0°C and at $10,000^\circ\text{C}$. The ground state energy of hydrogen atom is -13.6 eV . (20%)

2. Consider the time dependent Schrödinger equation for free particles moving in one dimension:

$$-\frac{\hbar^2}{2m} \frac{\partial^2 \Psi}{\partial x^2} = i\hbar \frac{\partial \Psi}{\partial t}$$

The general solution of above equation can be given as: $\Psi(x, t) = A(p)e^{i(px - Et)/\hbar}$

where $\varepsilon = p^2/2m$ is the nonrelativistic kinetic energy and p is the momentum. Assuming the normalized distribution function of the momentum is Gaussian and can be expressed as:

$$A(p) = \sqrt{\frac{\sigma}{2\pi\sqrt{\pi}\hbar^2}} \exp\left[-\frac{\frac{1}{2}\sigma^2(p - p_0)^2}{\hbar^2}\right]$$

where σ and p_0 are the parameters of the Gaussian distribution. Please find the normalized wavefunction Ψ and Δx of the particles at $t = 0$. Note that $\int_{-\infty}^{\infty} \exp[-\frac{y^2}{a^2} + iby] dy = \sqrt{\pi} a \exp[-(\frac{ab}{2})^2]$ (20%)

Plank constant $h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s}$

Boltzmann constant $k = 1.38 \times 10^{-23} \text{ J/K}$

Velocity of light $c = 300,000 \text{ Km/s}$

Electronic charge $e = 1.6 \times 10^{-19} \text{ C}$

Electron mass $m_e = 9.1 \times 10^{-31} \text{ kg}$

Proton mass $M = 1.67 \times 10^{-27} \text{ kg}$

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科目名稱：電子學【光電所碩士班選考】

題號：435004

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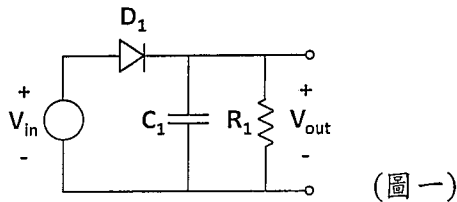
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一、簡答題 (40%)

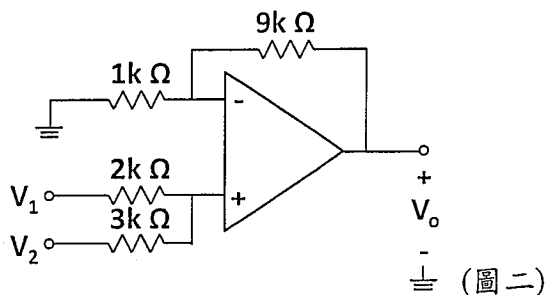
1. (10%) 請說明 pn 接面中空乏區(depletion region)的成因及空乏區寬度與雜質摻雜濃度、外加偏壓間的關係。
2. (10%) 請說明 Early effect 的成因及其對 BJT 操作特性的影響。
3. (10%) 請說明 Body effect 的成因及其對 MOS 操作特性的影響。
4. (10%) 請畫出 MOS 的結構圖，並說明通道(channel)的產生原理。

二、計算題(60%)

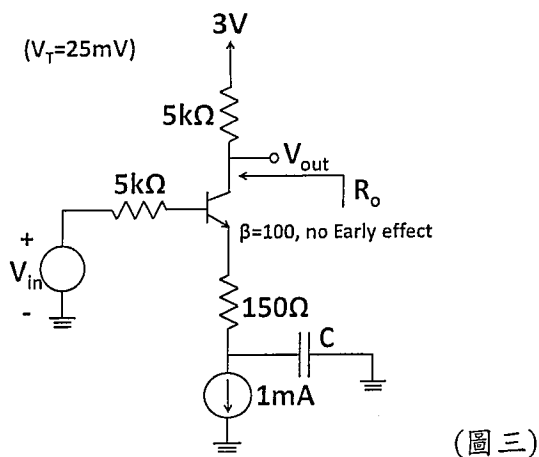
1. (10%) 圖一為一常見的整流電路，電路中的二極體啟動電壓(turn-on voltage)為 0.8V，電路中的輸入電壓是一個正弦波(峰值 $>0.8V$)，請將其輸出電壓(V_{out})波形與輸入電壓(V_{in})波形對時間作圖繪出。請討論此電路中電容(C_1)大小對其輸出電壓波形之影響。



2. (10%) 請推導出圖二電路的輸出電壓 V_o 與輸入電壓 V_1 、 V_2 間的關係。



3. (10%) 請計算出圖三電路的放大增益($A_o = V_{out}/V_{in}$)與輸出阻抗(R_o)。



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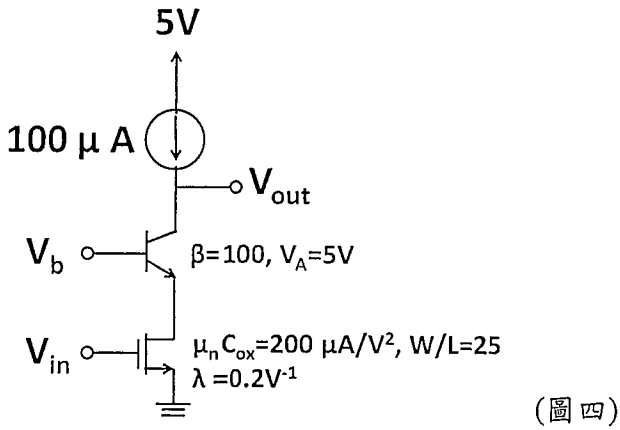
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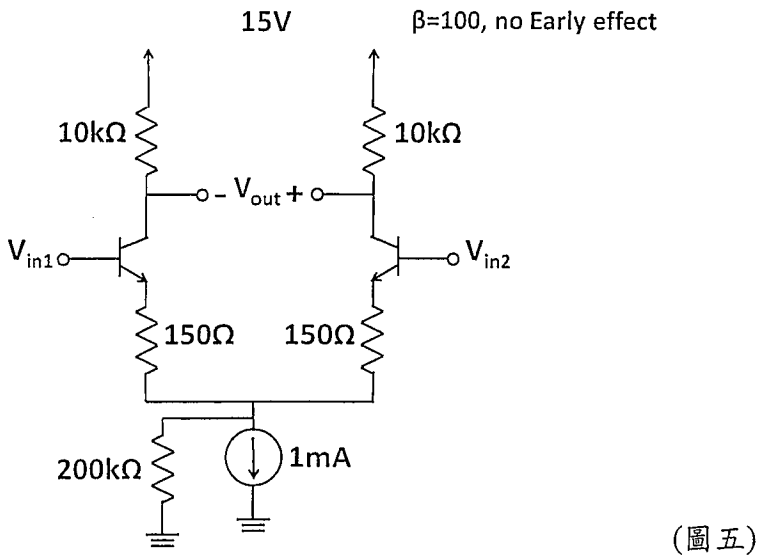
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4.(10%)請計算出圖四電路中的放大增益($A_o=V_{out}/V_{in}$)與輸出阻抗(R_o)。



5.(10%)請求出圖五電路的差動電壓增益 $V_{out}/(V_{in1}-V_{in2})$ 。



6.(10%)請求出圖六電路的-3db bandwidth。

