

**II. Questions (50%):**

1. An EM field oscillated at 1 GHz is excited in a lossy medium. The amplitude of the field is 100 V/m. The resistivity of the medium is  $1000 \Omega\text{m}$ . Please find the power dissipated per unit volume in the medium (6%).
2. For a rectangular waveguide having sides  $a$  and  $b$ , please draw the surface current of  $\text{TE}_{10}$  mode on the guide walls (8%).
3. Please define the magnetic susceptibility and relative permeability (5%).
4. The attenuation of a  $50 \Omega$  distortionless transmission line is  $0.0002 \text{ dB/cm}$ . The line has a capacitance of  $50 \mu\text{F}$ . Please find the velocity of wave propagation(6%).
5. Please plot the E-plane and H-plane radiation pattern of a Hertzian dipole (6%).
6. Dry air, glass, mineral oil, water (resistivity  $\sim 100 \text{ k}\Omega/\text{cm}$ ) and Mica, please choose the two materials from above list with the highest dielectric strength (8%).
7. A battery can deliver 1A of current for 100 hours. How much transfer of charges does this correspond to (5%)?
8. Please draw the electrical field lines of an electric dipole and magnetic flux line of a magnetic dipole (6%).

## I. Problems (50%) :

1. In Fig. 1, an TE polarized EM wave is propagating from medium 1 toward medium 2. The indices of the mediums are  $n_1$  and  $n_2$ , respectively. If the incident angle  $\theta_i$  is larger than the critical angle, please find the energy of the wave propagating along the x and z directions. Use Poynting theorem to verify your answers (20%).

$$\vec{E}_{in} = \hat{a}_y A e^{ikx} e^{-kz} \quad n_1 > n_2$$

Fig. 1

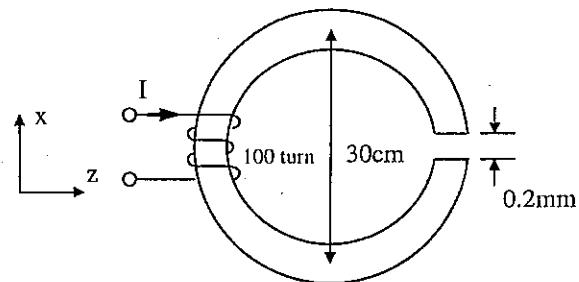
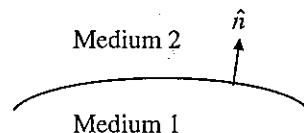


Fig. 2

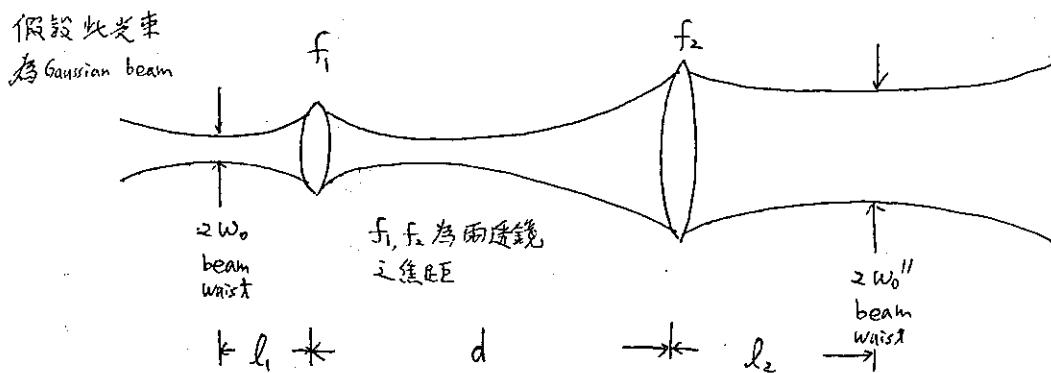
2. As shown in Fig. 2, a coil of 100 turns is wound around an iron ring ( $\mu_r = 4000$ ). The diameter and cross section of the ring are 30 cm and  $16 \text{ cm}^2$ , respectively. The ring contains an 0.2 mm wide air gap. If the gap is small enough so that the fringing effects in the air gap can be ignored, please calculate the force acting between the pole pieces of the ring when  $I = 1\text{A}$  (15%).
3. As shown in Fig. 3, S is the surface which bounds medium 1 from medium 2. Please show that the conservation of charge requires that

$$-\frac{\partial \rho_s}{\partial t} = (\vec{J}_2 - \vec{J}_1) \cdot \hat{n} + \nabla \cdot \vec{K}$$

Where  $\vec{J}_{1,2}$  are the volume current density,  $\vec{K}$  is the surface current density,  $\rho_s$  is the surface charge density and  $\hat{n}$  is the unit normal vector pointing from medium 1 to medium 2 (15%).



- 一、考慮如下圖之光束放大器 (beam expander), 若  $d = f_1 + f_2$ , 試計算其 beam size 的放大率, ( $\frac{w_0''}{w_0}$ ). (20分)



- 二、試說明何謂光波片 (wave retarder), 及其工作原理。 (20分)

- 三、以 1mW 之雷射穿過二個理想之線極化器 (linear polarizer), 其 transmission angle 分別為  $0^\circ$  及  $60^\circ$ , 試問輸出功率為何? 若在此二線極化器中間加入第三個線極化器, 其 transmission angle 為  $30^\circ$ , 則輸出功率為何? [假設三個線極化器均對雷射之波長有金屬上抗反射膜 (anti-reflection coating)] (20分)

- 四、試畫一簡要之 4 階雷射之能階圖, 並說明其工作原理。 (20分)

- 五、對 homogeneously broaded 的連續光雷射, 其輸出之中心波長是由 frequency pulling effect 決定, 試解釋何謂 frequency pulling effect. (20分)

1. Explain the following terms:

- (a) Zeeman effect. (10%)  
(b) Wien's law. (10%)

2. Consider an electron with energy  $E$  coming from left of the potential barrier

$$V(x) = V_0, x \geq 0$$

$$V(x) = 0, x < 0$$

Find the probability for the electron to transmit through the barrier.

- (a)  $E > V_0$ . (10%)  
(b)  $E < V_0$ . (10%)

3. The kinetic energy of a particle is equal to  $n$  times of its rest mass energy.

Find the particle's speed and momentum. (20%)

4. A particle of mass  $m$  moves one-directionally to the right of a hard wall at  $x = 0$  in a potential  $V(x)$ , where

$$V(x) = -B, 0 < x < b, B > 0;$$

$$V(x) = 0, x > b.$$

For fixed  $b$ , there is a minimum value of  $B$  below which there are no bound states.

Find this minimum,  $B_{min}$ . (20%)

5. For particle statistics, there are three distribution functions: Maxwell-Boltzmann, Bose-Einstein, and Fermi-Dirac distributions.

- (a) What are the particle properties of each distribution? For each distribution, give an example of the particles. (10%)  
(b) Write down the three distribution functions. (10%)

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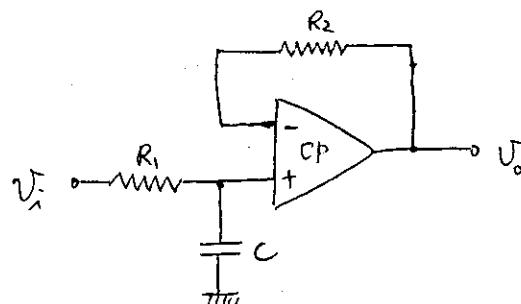
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## 一. 簡答題 (共 40 分)

1. 何謂 common-mode rejection ratio (CMRR) ? (10 分)
2. 何謂 sequential digital circuit ? (10 分)
3. 何謂 multiplexer 及 demultiplexer ? (10 分)
4. 為何 CMOS 電路比 PMOS 或 NMOS 電路省電 ? (10 分)

## 二. 計算及問答題 (共 60 分)

1. 考慮如下圖之 OP 放大器電路，試求出其 transfer function ( $\frac{V_o}{V_i}$ )，

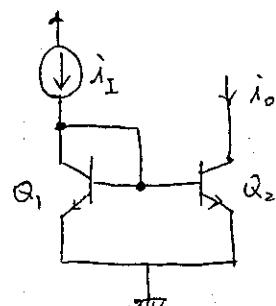


並大略繪出其頻率響應，此電路有何作用？(20 分)

[假設吋為理想之 op 放大器]

2. 对 -depletion type 之 MOSFET，在固定  $V_{GS}$  的情況下，繪出  $i_D$  與  $V_{DS}$  之關係，並解釋此曲線。[少用算式，多用文字或圖形以說明原理] (20 分)

3. 考慮如下圖之電路， $i_1$  為定電流源， $Q_1, Q_2$  為相同特性之



電晶體，其小信號增益為  $\beta$ ，試計算  $i_o$  與  $i_1$  之關係，此電路有何作用？(20 分)